

Solution to exercise 7:

7. Use the dataset in Exercise 6. Let  $\text{min\_sup}=3$  and the minimum confidence  $\text{min\_conf}=70\%$ . Use the Apriori Algorithm to discover all the strong association rules. Note that in this case, a strong association rule  $A \rightarrow B$  tells us that if a user visits certain set of pages A, the user has a high likelihood to visit the set of pages B.

- T1: {P1,P2,P3,P5,P7}
- T2: {P1,P4,P5,P6,P7}
- T3: {P1,P4,P6}
- T4: {P1,P4,P5,P6,P7}
- T5: {P3,P5}
- T6: {P1,P2,P3,P7}
- T7: {P2,P7}
- T8: {P1,P2,P3,P4,P6,P7}

Transaction	Itemsets
T1	{1,2,3,5,7}
T2	{1,4,5,6,7}
T3	{1,4,6}
T4	{1,4,5,6,7}
T5	{3,5}
T6	{1,2,3,7}
T7	{2,7}
T8	{1,2,3,4,6,7}

Step1: generating 1 Item set frequent pattern

1-Itemset	Sup_count
{1}	6
{2}	4
{3}	4
{4}	4
{5}	4
{6}	4
{7}	6

Scan the data once to get the count of each item and remove the items that do not meet  $\text{min\_sup}$

1-Itemset	Sup_count
{1}	6
{2}	4
{3}	4
{4}	4
{5}	4
{6}	4
{7}	6

**C1**

**L1**

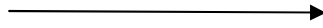
The set of frequent 1-itemsets, L1, consists of the candidate 1-itemsets satisfying minimum support.

In the first iteration of the algorithm, each item is a member of the set of candidate.

### Generating 2-itemset Frequent Pattern

2-Itemsets	Sup_Count
{1,2}	3
{1,3}	3
{1,4}	4
{1,5}	3
{1,6}	4
{1,7}	5
{2,3}	3
{2,4}	1
{2,5}	1
{2,6}	1
{2,7}	4
{3,4}	1
{3,5}	2
{3,6}	1
{3,7}	3
{4,5}	2
{4,6}	4
{4,7}	3
{5,6}	2
{5,7}	3
{6,7}	3

Scan the data set again for the support count of C2 and **remove** the non frequent itemsets from c2 --> L2



2-Itemsets	Sup_count
{1,2}	3
{1,3}	3
{1,4}	4
{1,5}	3
{1,6}	4
{1,7}	5
{2,3}	3
{2,7}	4
{3,7}	3
{4,6}	4
{4,7}	3
{5,7}	3
{6,7}	3

**L2**

**C2 (L1 X L1)**

### Step 3: Generating 3-item frequent set

From L2 to C3

3-itemsets	Sup_count
{1,2,3}	3
{1,2,7}	3
{1,3,7}	3
{1,4,6}	4
{1,4,7}	3
{1,5,7}	3
{1,6,7}	3
{2,3,7}	3
{4,6,7}	3

Reduce the size of C3 using the apriori property (any k-1) subset of a candidate must be frequent. Scan the dataset to get the support count

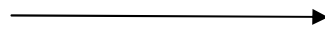
3-Itemsets	Sup_count
{1,2,3}	3
{1,2,7}	3
{1,3,7}	3
{1,4,6}	4
{1,4,7}	3
{1,5,7}	3
{1,6,7}	3
{2,3,7}	3
{4,6,7}	3

L3

C3 (L2 X L2)

### Step 4: generating 4 item frequent sets:

4-itemsets	Sup_count
{1,2,3,7}	3
{1,4,6,7}	3



4-Itemsets	Sup_count
{1,2,3,7}	3
{1,4,6,7}	3

L4

C4

C5 =  $\phi$  since the join of L4 and L4 doesn't generate any 5- itemsets and the algorithm terminates having found all the frequent item sets

These frequent itemsets are used to generate strong rules which satisfy both minimum support (3) and minimum confidence(70%).

Generating Association Rules from Frequent item sets

For each frequent itemset l, generate all nonempty subsets of l. For every nonempty subset of s of l, output rule  $s \Rightarrow (l-s)$  if  $\text{conf}(s \Rightarrow (l-s)) \geq \text{min\_conf}$ .

The frequent itemsets in this case are {1,2,3,7} and {1,4,6,7}

For itemset {1,2,3,7} all the non empty subsets are

{1}, {2}, {3}, {7}, {1,2}, {1,3}, {1,7}, {2,3}, {2,7}, {3,7} {1,2,3}, {1,2,7}, {2,3,7}, {1,3,7}

Let's take  $I = \{1,2,3,7\}$

Min confidence = 70%

Rule	$s \Rightarrow (I-s)$	Confidence	Selected/Rejected
R1	$1 \Rightarrow (2,3,7)$	$sc\{1,2,3,7\}/sc\{1\} = 3/6 = 50\%$	Rejected
R2	$2 \Rightarrow (1,3,7)$	$sc\{1,2,3,7\}/sc\{2\} = 3/4 = 75\%$	Selected
R3	$3 \Rightarrow (1,2,7)$	$sc\{1,2,3,7\}/sc\{3\} = 3/4 = 75\%$	Selected
R4	$7 \Rightarrow (1,2,3)$	$sc\{1,2,3,7\}/sc\{7\} = 3/6 = 50\%$	Rejected
R5	$(1,2) \Rightarrow (3,7)$	$sc\{1,2,3,7\}/sc\{1,2\} = 3/3 = 100\%$	Selected
R6	$(1,3) \Rightarrow (2,7)$	$sc\{1,2,3,7\}/sc\{1,3\} = 3/3 = 100\%$	Selected
R7	$(1,7) \Rightarrow (2,3)$	$sc\{1,2,3,7\}/sc\{1,7\} = 3/5 = 60\%$	Rejected
R8	$(2,3) \Rightarrow (1,7)$	$sc\{1,2,3,7\}/sc\{2,3\} = 3/3 = 100\%$	Selected
R9	$(2,7) \Rightarrow (1,3)$	$sc\{1,2,3,7\}/sc\{2,7\} = 3/4 = 75\%$	Selected
R10	$(3,7) \Rightarrow (1,2)$	$sc\{1,2,3,7\}/sc\{3,7\} = 3/3 = 100\%$	Selected
R11	$(1,2,3) \Rightarrow 7$	$sc\{1,2,3,7\}/sc\{1,2,3\} = 3/3 = 100\%$	Selected
R12	$(1,2,7) \Rightarrow 3$	$sc\{1,2,3,7\}/sc\{1,2,7\} = 3/3 = 100\%$	Selected
R13	$(1,3,7) \Rightarrow 2$	$sc\{1,2,3,7\}/sc\{1,3,7\} = 3/3 = 100\%$	Selected
R14	$(2,3,7) \Rightarrow 1$	$sc\{1,2,3,7\}/sc\{2,3,7\} = 3/3 = 100\%$	Selected

In this way we have found 11 strong rules

For itemset {1,4,6,7} all the non empty subsets are

{1}, {4}, {6}, {7}, {1,4}, {1,6}, {1,7}, {4,6}, {4,7}, {6,7} {1,4,6}, {1,4,7}, {1,6,7}, {4,6,7}

Let's take  $I = \{1,4,6,7\}$

Rule	$s \Rightarrow (I-s)$	Confidence	Selected/Rejected
R1	$1 \Rightarrow (4,6,7)$	$sc\{1,4,6,7\}/sc\{1\} = 3/6 = 50\%$	Rejected
R2	$4 \Rightarrow (1,6,7)$	$sc\{1,4,6,7\}/sc\{4\} = 3/4 = 75\%$	Selected
R3	$6 \Rightarrow (1,4,7)$	$sc\{1,4,6,7\}/sc\{6\} = 3/4 = 75\%$	Selected
R4	$7 \Rightarrow (1,4,6)$	$sc\{1,4,6,7\}/sc\{7\} = 3/6 = 50\%$	Rejected
R5	$(1,4) \Rightarrow (6,7)$	$sc\{1,4,6,7\}/sc\{1,4\} = 3/4 = 75\%$	Selected
R6	$(1,6) \Rightarrow (4,7)$	$sc\{1,4,6,7\}/sc\{1,6\} = 3/4 = 75\%$	Selected
R7	$(1,7) \Rightarrow (4,6)$	$sc\{1,4,6,7\}/sc\{1,7\} = 3/5 = 60\%$	Rejected
R8	$(4,6) \Rightarrow (1,7)$	$sc\{1,4,6,7\}/sc\{4,6\} = 3/4 = 75\%$	Selected
R9	$(4,7) \Rightarrow (1,6)$	$sc\{1,4,6,7\}/sc\{4,7\} = 3/3 = 100\%$	Selected
R10	$(6,7) \Rightarrow (1,4)$	$sc\{1,4,6,7\}/sc\{6,7\} = 3/3 = 100\%$	Selected
R11	$(1,4,6) \Rightarrow 7$	$sc\{1,4,6,7\}/sc\{1,4,6\} = 3/4 = 75\%$	Selected
R12	$(1,4,7) \Rightarrow 6$	$sc\{1,4,6,7\}/sc\{1,4,7\} = 3/3 = 100\%$	Selected
R13	$(1,6,7) \Rightarrow 4$	$sc\{1,4,6,7\}/sc\{1,6,7\} = 3/3 = 100\%$	Selected
R14	$(4,6,7) \Rightarrow 1$	$sc\{1,4,6,7\}/sc\{4,6,7\} = 3/3 = 100\%$	Selected

In this way we have found, 11 strong rules.

There will be total of 22 strong rules.