

Before split, the Entropy(D) is $E = -((1/3) * \log_2(1/3) + (1/5)*\log_2(1/5) + (1/5)*\log_2(1/5) + (2/15)*\log_2(2/15) + (2/15)*\log_2(2/15)) = 0.528 + 0.929 + 0.775 = 2.232$

1) if we split on body temperature:

For warm-blooded, there are 7 animals total, which have 5 mammals, and 2 birds, so the entropy for $D_1 = -((5/7)*\log_2(5/7) + (2/7)*\log_2(2/7)) = 0.863$

For cold-blooded, there are 8 animals total, which have 3 reptiles, 3 fishes, and 2 amphibian. So the entropy for $D_2 = -((3/8)*\log_2(3/8) + (3/8)*\log_2(3/8) + (1/4)*\log_2(1/4)) = 1.561$.

So Gain (body temperature) = $2.232 - ((7/15)*0.863 + (8/15)*1.561) = 0.997$

SplitInfo (body temperature) = $-((7/15)*\log_2(7/15) + (8/15)*\log_2(8/15)) = 0.997$

GainRatio (body temperature) = Gain (body temperature) / splitInfo (body temperature) = 1.0

2) If we split on skin cover:

For hair: there are 3 animals total, all of them are mammals,

So entropy for $D_1 = -1 * \log_2 1 = 0$.

For scales: there are 6 animals total, which have 3 reptiles and 3 fish,

So entropy for $D_2 = -((1/2) * \log_2(1/2) + (1/2)*\log_2(1/2)) = 1$.

For none: there are 2 animals total, all of them are amphibian, so entropy for $D_3 = 0$.

For feathers: there are 2 animals total, all of them are bird, so entropy for $D_4 = 0$.

For fur: there is 1 animal only, so the entropy for $D_5 = 0$.

For quill: there is 1 animal only, so the entropy for $D_6 = 0$.

So Gain(skin cover) = $2.232 - (6/15)*1 = 1.832$

SplitInfo (skin cover) = $-((3/15)*\log_2(3/15) + (6/15)*\log_2(6/15) + (2/15)*\log_2(2/15) + (2/15)*\log_2(2/15) + (1/15)*\log_2(1/15) + (1/15)*\log_2(1/15)) = 2.289$

GainRatio(skin cover) = $1.832/2.289 = 0.800$

3) If we split on gives birth:

For yes: there are 6 animals total, which have 5 mammals and 1 fish,

So the entropy for $D_1 = -((5/6)*\log_2(5/6) + (1/6)*\log_2(1/6)) = 0.65$.

For no: there are 9 animals total, which have 3 reptile, 2 fish, 2 amphibian and 2 birds.

So the entropy for $D_2 = -((3/9)*\log_2(3/9) + (2/9)*\log_2(2/9) + (2/9)*\log_2(2/9) + (2/9)*\log_2(2/9)) = 1.975$

So Gain(gives birth) = $2.232 - ((6/15)*0.65 + (9/15)*1.975) = 0.787$

SplitInfo(gives birth) = $-((6/15)*\log_2(6/15) + (9/15)*\log_2(9/15)) = 0.971$

GainRatio(gives birth) = $0.787 / 0.971 = 0.810$

4) If we split on Aquatic Creature:

For no: there are 7 animals total, which have 4 mammals, 2 reptiles, 1 bird,

So the entropy for $D_1 = -((4/7)*\log_2(4/7) + (2/7)*\log_2(2/7) + (1/7)*\log_2(1/7)) = 1.378$

For yes: there are 4 animals total, which have 3 fish and 1 mammal,

So the entropy for $D_2 = -((3/4)*\log_2(3/4) + (1/4)*\log_2(1/4)) = 0.811$

For semi: there are 4 animals total, which have 2 amphibians, 1 reptile and 1 bird.

So the entropy for $D_3 = -((2/4)*\log_2(2/4) + (1/4)*\log_2(1/4) + (1/4)*\log_2(1/4)) = 1.5$

So $\text{Gain}(\text{Aquatic Creature}) = 2.232 - ((7/15)*1.378 + (4/15)*0.811 + (4/15)*1.5) = 0.973$

$\text{SplitInfo}(\text{Aquatic Creature}) = -((7/15)*\log_2(7/15) + (4/15)*\log_2(4/15) + (4/15)*\log_2(4/15)) = 1.53$

$\text{GainRatio}(\text{Aquatic Creature}) = 0.973/1.53 = 0.636$

5) If we split on Aerial Creature:

For yes: there are 2 animals total, which have 1 mammal and 1 bird.

So the entropy for $D_1 = -((1/2)*\log_2(1/2) + (1/2)*\log_2(1/2)) = 1$

For no: there are 13 animals total, which have 4 mammals, 3 reptiles, 2 fish, 2 amphibians, and 2 reptiles,

So the entropy for $D_2 = -((4/13)*\log_2(4/13) + (3/13)*\log_2(3/13) + (2/13)*\log_2(2/13) + (2/13)*\log_2(2/13) + (2/13)*\log_2(2/13)) = 2.257$

So $\text{Gain}(\text{Aerial Creature}) = 2.232 - ((2/15)*1 + (13/15)*2.257) = 0.143$

$\text{SplitInfo}(\text{Aerial Creature}) = -((2/15)*\log_2(2/15) + (13/15)*\log_2(13/15)) = 0.567$

$\text{GainRatio}(\text{Aerial Creature}) = 0.143 / 0.567 = 0.252$

6) If we split on has legs:

For yes: there are 10 animals, which have 4 mammals, 2 amphibians, 2 reptiles and 2 birds,

So the entropy for $D_1 = -((4/10)*\log_2(4/10) + (2/10)*\log_2(2/10) + (2/10)*\log_2(2/10) + (2/10)*\log_2(2/10)) = 1.922$

For no: there are 5 animals total, which have 1 reptile, 3 fish and 1 mammal,

So the entropy for $D_2 = -((1/5)*\log_2(1/5) + (3/5)*\log_2(3/5) + (1/5)*\log_2(1/5)) = 1.371$

So $\text{Gain}(\text{has legs}) = 2.232 - ((10/15)*1.922 + (5/15)*1.371) = 0.495$

$\text{SplitInfo}(\text{has legs}) = -((10/15)*\log_2(10/15) + (5/15)*\log_2(5/15)) = 0.918$

$\text{GainRatio}(\text{has legs}) = 0.495/0.918 = 0.539$

7) If we split on Hibernates:

For yes: there are 5 animals total, which have 1 reptile, 2 amphibians, 2 mammals.

So the entropy for $D_1 = -((1/5)*\log_2(1/5) + (2/5)*\log_2(2/5) + (2/5)*\log_2(2/5)) = 1.522$

For no: there are 10 animals total, which have 3 mammals, 3 fish, 2 reptiles, and 2 birds.

So the entropy for $D_2 = -((3/10)*\log_2(3/10) + (3/10)*\log_2(3/10) + (2/10)*\log_2(2/10) + (2/10)*\log_2(2/10)) = 1.971$

So $\text{Gain}(\text{Hibernate}) = 2.232 - ((5/15) * 1.522 + (10/15) * 1.971) = 0.411$
 $\text{SplitInfo}(\text{Hibernate}) = -((5/15) * \log_2(5/15) + (10/15) * \log_2(10/15)) = 0.918$
 $\text{GainRatio}(\text{Hibernate}) = 0.411/0.918 = 0.448$

So we will split on Body Temperature.